

Technical Appendix for “Central Bank Communication and Expectations Stabilization”

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Abstract

This technical appendix provides the microfoundations and some calculations underlying the model in the paper.

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1 A Simple Model

The following details a simple model of output gap and inflation determination that is similar in spirit to Goodfriend and King (1997), Rotemberg and Woodford (1999) and Svensson and Woodford (2005). A continuum of households face a canonical consumption allocation problem and decide how much to consume of available differentiated goods and how much labor to supply to firms for the production of such goods. A continuum of monopolistically competitive firms produce differentiated goods using labor as the only input and face a price setting problem of the kind proposed by Rotemberg (1982).¹ The major difference is the incorporation of non-rational beliefs, delivering an anticipated utility model. The analysis follows Marcet and Sargent (1989) and Preston (2005), solving for optimal decisions conditional on current beliefs. Various mechanisms of persistence, such as habit formation, price indexation and inertial monetary policy are abstracted from. This provides sharp, perspicuous analytical results.² An earlier version of this paper, Eusepi and Preston (2008a), demonstrates that our conclusions regarding the value of communication in policy design remain pertinent in models with such modifications.

1.1 Microfoundations

Households. Households maximize their intertemporal utility derived from consumption and leisure

$$\hat{E}_{t-1}^i \sum_{T=t}^{\infty} \beta^{T-t} [\ln C_T^i - h_T^i]$$

subject to the flow budget constraint

$$B_t^i \leq R_{t-1} B_{t-1}^i + W_t h_t^i + P_t \Pi_t - P_t C_t^i - T_t^i$$

where B_t^i denotes holdings of the one period riskless bond, R_t denotes the gross interest paid on the bond, W_t the nominal wage, h_t^i labor supplied by household i and T_t^i lump-sum taxes

¹An analysis of price setting of the kind proposed by Calvo (1983), as implemented by Yun (1996), would lead to similar conclusions.

²It is also motivated by Milani (2007) and Eusepi and Preston (2008b) which suggest that purely forward looking business cycle models with learning dynamics provide a superior characterization of various U.S. macroeconomic time series than do rational expectations models with various persistence mechanisms.

and transfers for household i . Financial markets are assumed to be incomplete and Π_t denotes profits from holding shares in an equal part of each firm. Nominal income in any period t is $P_t Y_t^i = W_t h_t^i + P_t \Pi_t$ and P_t is the aggregate price level defined below. \hat{E}_t^i denote the beliefs at time t held by each household i , which satisfy standard probability laws. Section 3 describes the precise form of these beliefs and the information set available to agents in forming expectations. However, two points are worth noting. First, in forming expectations, households and firms observe only their own objectives, constraints and realizations of aggregate variables that are exogenous to their decision problems and beyond their control. They have no knowledge of the beliefs, constraints and objectives of other agents in the economy: in consequence agents are heterogeneous in their information sets in the sense that even though their decision problems are identical, they do not know this to be true. Second, given the assumed conditioning information for expectations formation, consumption plans are made one period in advance and therefore predetermined.³ Labor supply decisions are not predetermined and are conditioned on period t information.⁴

Each household consumes a composite good

$$C_t^i = \left[\int_0^1 c_t^i(j)^{\frac{\theta_t-1}{\theta_t}} dj \right]^{\frac{\theta_t}{\theta_t-1}}$$

which is made of a continuum of differentiated goods, $c_t^i(j)$, each produced by a monopolistically competitive firm j . The elasticity of substitution among differentiated goods, θ_t , is time-varying, with $E[\theta_t] = \theta > 1$. This is a simple way of modeling time-varying mark-ups, introducing a trade-off between inflation and output stabilization relevant to optimal policy design.

A log-linear approximation to the first order conditions of the household problem provides the household Euler equation

$$\hat{C}_t^i = \hat{E}_{t-1} \left[\hat{C}_{t+1}^i - (\hat{i}_t - \pi_{t+1}) \right] \quad (1)$$

³We consider a model with pricing and spending decisions determined one period in advance so as to put households, firms and policymakers on an identical informational footing. This could similarly be achieved by the alternative assumption that the central bank has a policy reaction function that responds to one period ahead expectations of inflation and agents condition decisions on period t information. All results continue to hold.

⁴This assumption ensures markets clear in equilibrium.

and the intertemporal budget constraint

$$\hat{E}_{t-1} \sum_{T=t}^{\infty} \beta^{T-t} \hat{C}_T^i = \omega_{t-1}^i + \hat{E}_{t-1} \sum_{T=t}^{\infty} \beta^{T-t} \hat{Y}_T^i \quad (2)$$

where

$$\hat{Y}_t \equiv \ln(Y_t/\bar{Y}); \hat{C}_t \equiv \ln(C_t/\bar{C}); \hat{w}_t \equiv \ln(R_t/\bar{R}); \pi_t = \ln(P_t/P_{t-1}); \omega_t^i = B_t^i/\bar{Y};$$

and \bar{z} denotes the steady state value of any variable z .

Solving the Euler equation recursively backwards, taking expectations at time $t - 1$ and substituting into the intertemporal budget constraint gives

$$\hat{C}_t^i = (1 - \beta) \omega_{t-1}^i + \hat{E}_{t-1} \sum_{T=t}^{\infty} \beta^{T-t} \left[(1 - \beta) \hat{Y}_T^i - \beta(i_T - \pi_{T+1}) \right]. \quad (3)$$

Optimal consumption decisions depend on current wealth at the beginning of the period, ω_{t-1}^i , and on the expected future path of income and the real interest rate.⁵ The optimal allocation rule is analogous to permanent income theory, with differences emerging from allowing variations in the real rate of interest, which can occur either due to variations in the nominal interest rate or inflation. Nominal interest rates affect consumption demand only through expectations. Moreover, consumption decisions depend on the *entire expected future path of the nominal interest rate*, in contrast with Bullard Mitra (2002) and Orphanides and Williams (2005), among others, where only the current interest rate matters for output determination. This property underscores the role of managing expectations in policy design. Note also, that as households become more patient, current consumption demand is more sensitive to expectations about future macroeconomic conditions.

Firms. There is a continuum of monopolistically competitive firms. Each differentiated consumption good is produced according to the linear production function

$$Y_{j,t} = A_t h_{j,t}$$

⁵Using the fact that total household income is the sum of dividend and wage income, combined with the first order conditions for labor supply and consumption, delivers a decision rule for consumption that depends only on forecasts of prices: that is, goods prices, nominal interest rates, wages and dividends. However, we make the simplifying assumption that households forecast total income, the sum of dividend payments and wages received.

where A_t denotes an aggregate technology shock. Each firm chooses a price $P_{j,t}$ in order to maximize its expected discounted value of profits

$$\hat{E}_{t-1}^j \sum_{T=t}^{\infty} Q_{t,T} P_T \Pi_{j,T}$$

where

$$\Pi_{j,t} = (1 - \tau) \frac{P_{j,t}}{P_t} Y_{j,t} - \frac{W_t}{P_t} h_{jt} - \frac{\psi}{2} \left(\frac{P_{j,t}}{P_{j,t-1}} - 1 \right)^2$$

denotes period profits and the quadratic term the cost of adjusting prices as in Rotemberg (1982).⁶ The tax, τ , on revenues is chosen to eliminate the steady state distortion arising from monopolistic competition. Given the incomplete markets assumption it is assumed that firms value future profits according to the marginal rate of substitution evaluated at aggregate income

$$Q_{t,T} = \beta^{T-t} \frac{P_t Y_t}{P_T Y_T}$$

for $T \geq t$.⁷

The intratemporal consumer problem implies aggregate demand for each differentiated good is

$$Y_{jt} = \left(\frac{P_{j,t}}{P_t} \right)^{-\theta_t} Y_t$$

where Y_t denotes aggregate output and

$$P_t = \left[\int_0^1 (P_{j,t})^{1-\theta_t} dj \right]^{\frac{1}{1-\theta_t}}$$

is the associated price index. Summing up, the firm chooses a sequence for $P_{j,t}$ to maximize profits, given the constraint that demand should be satisfied at the posted price, taking as given P_t , Y_t , and W_t . Again, given the information upon which expectations are conditioned, prices are determined one period in advance.

⁶The results are similar to the case of a Calvo pricing model.

⁷The precise details of this assumption are not important to the ensuing analysis so long as in the log linear approximation future profits are discounted at the rate β^{T-t} .

The first-order condition to the firm's problem is

$$\begin{aligned} \hat{E}_{t-1} \left[\psi \left(\frac{P_{j,t}}{P_{j,t-1}} - 1 \right) \frac{P_t}{P_{j,t-1}} \right] &= \hat{E}_{t-1} \left[Q_{t,t+1} \psi \left(\frac{P_{j,t+1}}{P_{j,t}} - 1 \right) \frac{P_{j,t+1} P_t}{P_{j,t}^2} \right] \\ &+ \hat{E}_{t-1} \left[\theta_t Y_t \left(\frac{P_{j,t}}{P_t} \right)^{-\theta_t} \left(\left(\frac{P_{j,t}}{P_t} \right)^{-1} S_t - \frac{(\theta_t - 1)}{\theta_t} \right) \right]. \end{aligned}$$

A log-linear approximation provides

$$\hat{P}_{j,t} - \hat{P}_{j,t-1} = \beta \hat{E}_{t-1} [\hat{P}_{j,t+1} - \hat{P}_{j,t}] + \xi \hat{E}_{t-1} [\hat{s}_t + \hat{\mu}_t + \hat{P}_t - \hat{P}_{j,t}]$$

where $\hat{P}_t = \log P_t$; $\hat{P}_{j,t} = \log P_{j,t}$; $\xi \equiv (1 - \theta) \bar{Y} / \psi$; $\mu_t = \theta_t (\theta_t - 1)^{-1}$ denotes the mark-up and satisfies $\hat{\mu}_t = \ln(\mu_t / \bar{\mu})$; and $\hat{s}_t \equiv \ln(S_t / \bar{S})$ is marginal costs (defined below) in deviations from steady state. Collecting terms in the price of firm j provides

$$\left[1 - \left(\frac{\xi}{\beta} + \frac{1}{\beta} + 1 \right) L + \frac{1}{\beta} L^2 \right] \hat{E}_{t-1} \hat{P}_{j,t+1} = -\frac{\xi}{\beta} L \hat{E}_{t-1} [\hat{s}_{t+1} + \hat{\mu}_{t+1} + \hat{P}_{t+1}]$$

where L denotes the lag operator. Factoring the polynomial and solving the unstable root forward determines the optimal price of the firm as

$$\hat{P}_t(j) = \gamma_1 \hat{P}_{t-1}(j) + \xi \gamma_1 \hat{E}_{t-1} \sum_{T=t}^{\infty} (\gamma_1 \beta)^{T-t} [\hat{s}_T + \hat{\mu}_T + \hat{P}_T] \quad (4)$$

where the roots γ_1 and γ_2 satisfy

$$0 < \gamma_1 < 1, \quad \gamma_2 > 1, \quad \gamma_1 \gamma_2 = \beta^{-1} \quad \text{and} \quad \gamma_1 + \gamma_2 = \beta^{-1} (\xi + 1 + \beta).$$

The latter two properties combined imply $\xi = (1 - \gamma_1) (1 - \gamma_1 \beta) \gamma_1^{-1}$. Noting that

$$\hat{E}_{t-1} \sum_{T=t}^{\infty} \left(\frac{1}{\gamma_2} \right)^{T-t} \pi_T = -\hat{P}_{t-1} + \left(1 - \frac{1}{\gamma_2} \right) \hat{E}_{t-1} \sum_{T=t}^{\infty} \left(\frac{1}{\gamma_2} \right)^{T-t} \hat{P}_T$$

permits the optimal price decision to be written in terms of aggregate inflation as

$$\hat{P}_{j,t} = \gamma_1 \hat{P}_{j,t-1} + \left(1 - \frac{1}{\gamma_2} \right)^{-1} \frac{\xi}{\gamma_2 \beta} \left\{ P_{t-1} + \hat{E}_{t-1} \sum_{T=t}^{\infty} \left(\frac{1}{\gamma_2} \right)^{T-t} \left[\left(1 - \frac{1}{\gamma_2} \right) (\hat{s}_T + \hat{\mu}_T) + \pi_T \right] \right\}.$$

This condition states that each firm's current price depends on the expected future path of real marginal costs, the aggregate price level and cost-push shocks.⁸

⁸In an earlier version of this paper, Eusepi and Preston (2008a), the firm's decision problem was simplified by making certain assumptions about the information available to firms when setting prices. Mike Woodford and an anonymous referee are thanked for encouraging the authors to characterize the more general case presented here. The general tenor of results is unchanged.

The real marginal cost function is

$$S_t = \frac{w_t}{A_t} = \frac{C_t}{A_t}$$

where the second equality comes from the household's labor supply decision. Log-linearizing we obtain

$$\hat{s}_t = \hat{C}_t - \hat{a}_t,$$

so that current prices depend on expected future demand and technology. The responsiveness of current prices to changes in expected demand depends on the degree of nominal rigidity. A low degree of nominal rigidity implies a high value of ξ (corresponding to a low value of the cost ψ): in this case firms respond aggressively to changes in perceived demand because price changes are less costly. The opposite occurs in the case of higher costs of price adjustment. The degree of price rigidity plays a key role in the stability analysis.

1.2 Market clearing, efficient output and aggregate dynamics

The model is closed with assumptions on monetary and fiscal policy. The fiscal authority, aside from levying taxes to eliminate the steady state distortion from monopolistic competition, is assumed to follow a zero debt policy in every period t and this is understood to be true by agents.⁹ Monetary policy is discussed in detail in the subsequent section. For now it suffices to note that a nominal interest rate rule is implemented. For a more general treatment of the interactions of fiscal and monetary policy under learning dynamics see Eusepi and Preston (2008c) and Evans and Honkapohja (2007).

General equilibrium requires that the goods market clears, so that

$$A_t h_t - \frac{\psi}{2} (\Pi_t - 1)^2 = \int C_t dj = C_t. \quad (5)$$

This condition states that output net of adjustment costs is equal to aggregate consumption, determining the equilibrium demand for labor h_t at the wage $w_t = C_t$. This relation satisfies the log-linear approximation

$$\hat{h}_t + \hat{a}_t = \hat{C}_t = \hat{Y}_t.$$

⁹This implies agents do not need to forecast future tax obligations as in the analyses of Eusepi and Preston (2007b, 2007d).

It is useful to characterize the *efficient* level of output that would occur absent nominal rigidities and distortionary shocks *under rational expectations*. Under these assumptions, optimal price setting implies the log-linear approximation $E_{t-1}\hat{Y}_t^e = E_{t-1}\hat{a}_t$. Hence predictable movements in the efficient rate of output are entirely determined by the aggregate technology shock. Nominal bonds are also in zero net supply requiring

$$\int_0^1 B_t^i di = 0.$$

Aggregating firm and household decisions, using (3) and (4), provides

$$x_t = \hat{E}_{t-1} \sum_{T=t}^{\infty} \beta^{T-t} [(1 - \beta)x_T - \beta(i_T - \pi_{T+1}) + \beta\hat{r}_t^e] \quad (6)$$

and

$$\pi_t = \frac{\gamma_1 \xi}{(1 - \gamma_1 \beta)} \hat{E}_{t-1} \sum_{T=t}^{\infty} (\gamma_1 \beta)^{T-t} [(1 - \gamma_1 \beta)(x_T + \hat{\mu}_T) + \pi_T] \quad (7)$$

where $\int_0^1 \hat{E}_t^i di = \hat{E}_t$ gives average expectations; $x_t = \hat{Y}_t - E_{t-1}\hat{Y}_t^e$ denotes the log-deviation of output from its expected efficient level; and $\hat{r}_t^e = (\hat{Y}_{t+1}^e - \hat{Y}_t^e)$ the corresponding efficient rate of interest. The average expectations operator does not satisfy the law of iterated expectations due to the assumption of completely imperfect common knowledge on the part of all households and firms. Because agents do not know the beliefs, objectives and constraints of others in the economy, they cannot infer aggregate probability laws.

1.3 The Monetary Authority

The monetary authority minimizes a standard quadratic loss function under the assumption that agents have rational expectations. This approach follows a now substantial literature on learning dynamics and monetary policy — see Howitt (1992) for the seminal contribution and Bullard and Mitra (2002), Evans and Honkapohja (2003) and Preston (2006, 2008), *inter alia*, for subsequent contributions — motivated by the question of robustness of standard policy advice to small deviations from the rational expectations assumption. For alternative

treatments of policy design that exploit knowledge of private agent learning see Gaspar, Smets, and Vestin (2005), Molnar and Santoro (2005) and Preston (2006, 2008).

The optimal policy problem is

$$\min E_{t-1} \sum_{T=t}^{\infty} (\pi_T^2 + \lambda_x x_T^2)$$

subject to the constraints

$$x_t = E_{t-1} x_{t+1} - E_{t-1} (i_t - \pi_{t+1} - r_t^e) \quad (8)$$

$$\pi_t = \xi E_{t-1} x_t + \beta E_{t-1} \pi_{t+1} + E_{t-1} \hat{\mu}_t \quad (9)$$

which are the model implied aggregate demand and supply equations under rational expectations.¹⁰ The weight $\lambda_x > 0$ determines the relative priority given to output gap stabilization. A second-order accurate approximation to household welfare in this model can be shown to imply a specific value for λ_x . Because this is not central to our conclusions, and because this more general notation permits indexing a broader class of policy rules, we adopt this objective function.

The first-order condition under discretion is

$$E_{t-1} \pi_t = -\frac{\lambda_x}{\xi} E_{t-1} x_t. \quad (10)$$

Hence optimal policy dictates interest rates to be adjusted so that predictable movements in inflation are negatively related to those in the output gap.¹¹ This targeting rule combined with the structural relations (8) and (9) can be shown to determine the rational expectations equilibrium paths $\{i_t^*, \pi_t^*, x_t^*\}$ as linear functions of the exogenous state variables $\{r_{t-1}^e, \hat{\mu}_{t-1}\}$. Without loss of generality, and to make the analysis as simple and transparent as possible,

¹⁰These expressions follow directly from (6) and (7) on noting that \hat{E}_t satisfies the law of iterated expectations under the assumption of rational expectations — households and firms know the objectives, beliefs and constraints of other agents and can therefore determine aggregate probability laws in equilibrium. Also, at the rational expectations equilibrium $x_t = E_{t-1} x_t$ and $\pi_t = E_{t-1} \pi_t$. These equivalences are not true under learning.

¹¹Policies under optimal commitment could similarly be analyzed without substantial differences in the conclusions of this paper. However, because such policies introduce history dependence, analytical conditions are somewhat tedious and we therefore take the case of discretion for convenience.

we assume that the exogenous processes are determined by

$$\begin{aligned} r_t^e &= \rho_r r_{t-1}^e + \varepsilon_t^r \\ \hat{\mu}_t &= \rho_\mu \hat{\mu}_{t-1} + \varepsilon_t^\mu \end{aligned}$$

where $0 < \rho_r, \rho_\mu < 1$ and $(\varepsilon_t^r, \varepsilon_t^\mu)$ are independently and identically distributed random variables, with autoregressive coefficients known to households and firms.¹² Under these assumptions

$$i_t^* = \rho_r r_{t-1}^e + \phi_\mu \rho_\mu \hat{\mu}_{t-1}$$

where

$$\phi_\mu = \frac{\rho_\mu \lambda_x + (1 - \rho_\mu) \xi}{\xi^2 + \lambda_x (1 - \beta \rho_\mu)}$$

delineates the desired state contingent evolution of nominal interest rates required to implement the optimal equilibrium.

Following Svensson and Woodford (2005), rather than adopting the targeting rule (10) directly as the policy rule, we instead assume the central bank implements policy according to the nominal interest rate rule

$$i_t = i_t^* + \phi \left(\hat{E}_{t-1} \pi_t + \frac{\lambda_x}{\xi} \hat{E}_{t-1} x_t \right) \quad (11)$$

$$= i_t^* + \phi \hat{E}_{t-1} \pi_t + \phi_x \hat{E}_{t-1} x_t \quad (12)$$

where $\phi > 0$ and $\phi_x \equiv (\phi \lambda_x / \xi) > 0$. This serves to limit the information that the central bank requires to implement monetary policy. Moreover, an explicit policy rule can be learned by market participants without them specifying a complete model of the economy. The central bank is assumed to observe private forecasts — through survey data — or to have an identical internal forecasting model. This rule has the property that if beliefs converge to the underlying rational expectations equilibrium then it is consistent with implementing optimal policy under a rational expectations equilibrium. This follows immediately from observing in this case that

$$\hat{E}_{t-1} \pi_t + \frac{\lambda_x}{\xi} \hat{E}_{t-1} x_t = 0$$

¹²This assumption can be dispensed with without altering results. Because these shocks are exogenous and assumed to be observed by agents, it is immediate that estimating a first order process for each shock will recover the true autoregressive coefficient with probability going to one as the sample size goes to infinity.

which in turn implies $i_t = i_t^*$ as required for optimality under rational expectations. Note also that it nests an expectations-based Taylor rule as a special case, albeit with a stochastic constant.¹³

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¹³The stochastic constant is largely irrelevant to the stability analysis under learning dynamics. Also, if the assumption of discretionary optimization is unappealing, then a rule of this form with appropriately defined stochastic constant can implement the optimal equilibrium under commitment — see Preston (2006).

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